



TITLE:

7. Dissipation and the Dynamics of Macroscopic Quantum Systems

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RIGHT:

$$\text{Tr}(H^n) = \frac{\sum_{i_1 \dots i_n}^N H_{i_1 i_2} H_{i_2 i_3} \dots H_{i_n i_1}}{\left(\sum_i^N H_{ii}\right)^n}$$

を調べることによって展開基底に依存せずにも導かれる。行列要素間に全く相関がなく、 p 次のモーメントが m_p で与えられるような分布関数から得られる乱数の行列を考えると、そのトレースは、行列の次元 N が無限大の極限で、 $\text{tr}(H^2) = m_2/m_1$ である他は、 $\text{tr}(H^n) = 1 (n \geq 3)$ になる。われわれが調べた現実のハミルトニアンは、対角要素が、非対角要素に比べて、圧倒的に大きいことを反映して、上記の乱数行列とは、明らかに異なる(図1)。また、真のハミルトニアンから行列要素をわずかにずらす(隣りあう要素どうしをランダムに交換する。)ことにより、レベル間隔分布を特徴づける Brody parameter β は、4次同次形では、 $\beta = 0.91 \rightarrow 0.66$ 、モース系では、 $\beta = 0.40 \rightarrow 0.86$ というように、かわる場合がみられる。このことは、非対角要素にも要素間相関があることを示しているが、この性質も、展開基底に依存せずに、もともとの行列要素から直接把えることが可能かどうかは今後の課題であろう。

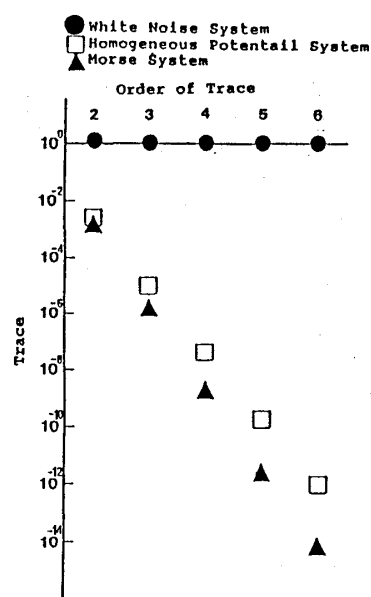


図1 規格化されたトレース

Reference

- 1) 首藤啓, 松下利樹 物性研究 48 巻 4 号

7. Dissipation and the Dynamics of Macroscopic Quantum Systems

北大・工 飛田和男

1. Introduction

In the dynamics of macroscopic systems, the dissipative effect is

unavoidable. Owing to the recent development of microfabrication technique, the quantum effect is being observed in the dynamics of macroscopic degrees of freedom such as the magnetic flux in SQUID which also obeys the dissipative dynamics. Caldeira and Leggett¹⁾ have given a theoretical formulation to include the Ohmic dissipation in the dynamics of macroscopic variables. Here we review their result and some examples of its applications. In the following, the explicit formulae are not given due to the limitation of length. For the details, see the references given at the end of the paper.

2. Quantum Tunnelling with Dissipation

In the single junction SQUID, the dynamics of the magnetic flux Φ confined in the ring is described by the equation of motion equivalent to that for the damped motion of a particle in the nonlinear potential.¹⁾ If the external magnetic flux is increased from zero to a certain finite value, the state with $\Phi = 0$ becomes metastable. It decays into the true ground state by thermal activation or quantum tunnelling. At low temperatures, the quantum tunnelling is dominant if the size of the junction is small enough. This tunnelling process is accompanied by dissipation. Caldeira and Leggett¹⁾ treated this process theoretically introducing the heat bath consisting of infinite number of harmonic oscillators linearly coupled to Φ . Using the imaginary time path integral formalism and eliminating the heat bath variables, they obtained the path integral expression for the thermodynamic quantities in terms of the effective action which is the functional only of Φ .

Using this action, the tunnelling rate Γ is calculated. It is shown that Γ is always reduced by dissipation. The recent experiments using small junctions of submicron size confirm their result quantitatively²⁾.

3. Quantum Coherence and Dissipation

If Φ is equal to $\Phi_0/2$ (Φ_0 : flux quantum), the states with $\Phi=0$ and Φ_0

are doubly degenerate ground states in the absence of tunnelling. In the usual quantum mechanics with tunnelling, the true ground state is the coherent superposition of the two states above. It is shown, however, that for sufficiently strong damping the coherence is destroyed and tunnelling probability vanishes. As a result, the system stays in one of the localized states. The theoretical treatment is given in 3). The experimental detection of coherent behavior is not yet successful and is one of the most challenging experiment in this field.

4. Dissipation and Chaos in Quantum Systems

While the chaotic orbit can attain a fine structure of any complexity in the classical systems, it is destroyed by the interference of wave function in the corresponding quantum systems, and the quantum-classical correspondence holds only for the rather short time scale $\tau_c \sim \ln \hbar^{-1}$ 4). The dissipative coupling with the heat bath can destroy the interference helping the recovery of the chaotic dynamics⁵⁾.

In the real time path integral representation of the quantum dynamics of the density matrix, two exponential factors appear corresponding to the time developments along forward and backward paths q_1 and q_2 . In the absence of dissipation, these paths can be arbitrarily apart and contribute to the integral with equal weight and various phase factors resulting in interference. The dissipative contribution to the action, however, suppresses the fluctuation in $y = q_1 - q_2$ reducing the interference between widely separated paths. The amplitude δy of the fluctuation in y is bounded by $\sqrt{\hbar C}$ (C : a constant determined by the heat bath). If C is finite, δy is bounded uniformly with respect to time and the interference is suppressed for arbitrary time in the limit $\hbar \rightarrow 0$. For the Ohmic heat bath, C is logarithmically divergent with respect to time. This divergence, however, is so weak that the convergence is uniform within practical time scale.

If δy is much smaller than the typical variation scale of nonlinear

potential, the interference is well reduced and the distribution of the paths is equivalent to that of the Brownian motion with the c-number quantum noise with colored time correlation^{5,6)}. This noise is the main quantum effect in the semiclassical dissipative system. Although the chaotic orbit is sensitive to the noise, the structure of the chaotic attractor would not be strongly affected by the noise if it is structurally stable enough. If it is not the case, however, the noise has dominating effect on the dynamics^{7,8)}.

5. Bloch Wave Oscillation in Josephson Junction

The oscillation corresponding the Bloch oscillation of a quantum particle in a ideal crystal is realized in Josephson junction in which the phase corresponds to the displacement of the particle and the charge to its momentum. For details, see 9)(theory) and 10)(experiment).

References

As reviews on the subjects in sections 1 - 3:

- A) A.J. Leggett: Proc. 2nd Int. Symp. Foundations of Quantum Mechanics in the Light of New Technology, ed. M. Namiki et al., (1987) 287.
- B) K. Hida: Butsuri 41, (1986) 875. (in Japanese)

For section 2:

- C) P. Hanggi: J. Stat. Phys. 42, (1986) 105.

For section 3:

- D) A.J. Leggett, S. Chakraverty, A.T. Dorsey, M.P.A. Fisher, A. Garg and W. Zwerger: Rev. Mod. Phys. 59, 1 (1987).

- 1) A.O. Caldeira and A.J. Leggett: Phys. Rev. Lett. 46, (1981) 211.; Ann. Phys. (NY) 149, (1983) 374; 153, (1984) 445(E)
- 2) A.N. Cleland, J.M. Martinis and J. Clarke: Jpn. J. Appl. Phys. 26, (1987) Suppl. 1427 (Proc. LT18).

研究会報告

- 3) S. Chakraverty: Phys. Rev. Lett. 49, (1982) 681; A.J. Bray and M.A. Moore: ibid. 1545.
- 4) M. Toda and K. Ikeda: to appear in Phys. Lett. (1987).
- 5) K. Hida: preprint(1987) .
- 6) A. Schmid: J. Low Temp. Phys. 49 (1982) 609.
- 7) K. Hida: J. Phys. Soc. Jpn. 55 (1986) 3694.
- 8) K. Hida: J. Phys. Soc. Jpn. 56 (1987) 2325.
- 9) K.K. Likharev and A.B. Zorin: J. Low Temp. Phys. 62, (1985) 345.
- 10) K. Yoshihiro, J. Kinoshita, K. Inagaki and C. Yamanouchi: same as A)298.

9. エアリード楽器の研究から

I フルートの発音における駆動条件限界値

II 尺八管の形状の微小変化が性能に及ぼす影響

九州芸術工科大学 安藤由典

講演者は昭和35年頃から、フルート、能管、尺八など「エアリード楽器」と呼ばれる一群の管楽器を調べている。ここではその中から、この研究会のメンバーに興味のありそうな、副題にあげた二つの話題について以下の目次に従って述べる。

I フルートの発音における駆動条件限界値

1. フルード研究の目的 フルードを吹鳴する駆動条件と発生音物理量との関係を明らかにする。
2. 駆動条件の項目、及びこれを実現する実験装置
3. 発音のための重要条件 唇の存在、呼気流の偏り(偏心)、偏心と低音吹鳴可能最大流速、偏心と倍音構造
4. 演奏家の音色個性の倍音構造における現れ
5. 研究の応用 望ましい吹口断面形の設定、断面形と駆動条件限界値との関係